

Q1. The relation R in the set of natural numbers N defined as $R = \{ (x, y) : y = x + 5 \text{ and } x < 4 \}$ is :

- (a) reflexive
- (b) symmetric
- (c) equivalence
- (d) none of these

Ans. (d) none of these

Explanation:

$$R = \{(1, 6), (2, 7), (3, 8)\}$$

$$\therefore (6, 6) \notin R$$

$\Rightarrow R$ is not Reflexive.

$$\text{For } (2, 7) \in R$$

$$\Rightarrow (2, 7) \in R \text{ but } (7, 2) \notin R$$

$\Rightarrow R$ is not symmetric.

Now, since there is no pair in R such that (x, y) and $(y, z) \in R$, then (x, z) cannot belong to R.

$\therefore R$ is transitive.

$\Rightarrow R$ is not equivalence

Q2. For the set $A = \{ 1, 2, 3 \}$, define a relation R in the set A as follows $R = \{ (1, 1), (2, 2), (3, 3), (1, 3) \}$ Then, the ordered pair to be added to R to make it the smallest equivalence relation is

- (a) (1, 3)
- (b) (3, 1)
- (c) (2, 1)
- (d) (1, 2)

Ans. (b) (3, 1)

Explanation:

$$(1, 1), (2, 2) \text{ and } (3, 3) \in R$$

$\Rightarrow R$ is Reflexive.

$$(1, 3) \in R$$

$$(1, 3) \in R \text{ but } (3, 1) \notin R$$

$\Rightarrow R$ is not symmetric.

To make R an equivalence we can add (3, 1).

Clearly R is reflexive and transitive. For R to be symmetric we should add (3, 1) in R.

Q3. Let $A = \{1, 2, 3\}$ and $B = \{a, b, c, d\}$. Which of the following relation from A to B is not a function?

- (a) $R_1 = \{(1, a), (2, b), (3, c)\}$
- (b) $R_2 = \{(1, a), (2, b), (3, d)\}$
- (c) $R_3 = \{(1, a), (1, b), (2, c), (3, d)\}$
- (d) $R_4 = \{(1, a), (2, c), (3, d)\}$

Ans. (c) $R_3 = \{(1, a), (1, b), (2, c), (3, d)\}$

Explanation:

R_3 is not a function since $1 \in A$ has two images $a, b \in B$. R_1 and R_2 are functions since in these relations, every element of A has a unique image in B .

Q4. Let $A = \{1, 2, 3\}$, $B = \{4, 5, 6, 7\}$ and let $f = \{(1, 4), (2, 5), (3, 6)\}$ be a function from A to B . State whether

- (a) f is one-one only
- (b) f is onto only
- (c) f is one one and onto both
- (d) none of these

Ans. (a) f is one-one only

Explanation:

Here, $f : A \rightarrow B$ is defined as $\{(1, 4), (2, 5), (3, 6)\}$.

Since the images of distinct elements of A under f are distinct as :

$$f(1) = 4, f(2) = 5 \text{ and } f(3) = 6$$

From above it is evident that $x_1 \neq x_2$ and $f(x_1) \neq f(x_2)$ i.e. $x_1 = x_2$ and $f(x_1) = f(x_2)$.

$f : A \rightarrow B$ is one-one.

Therefore, f is one-one only.

Q5. The number of all possible matrices of order 2×3 with each entry 1 or 2 is:

- (a) 64
- (b) 12
- (c) 36
- (d) 28

Ans. (a) 64

Explanation:

In a 2×3 matrix, the number of elements is 6.

Each place could have 2 elements.

$$\text{Total possible outcomes} = 2 \times 2 \times 2 \times 2 \times 2 = 64$$

Q6. If A and B are symmetric matrices of the same order, then $(AB - BA)$ is a:

- (a) Skew symmetric matrix
- (b) Null matrix
- (c) Symmetric matrix
- (d) None of these

Ans. (a) Skew symmetric matrix

Explanation:

Since A and B are symmetric matrices such that $A' = A$ and $B' = B$

$$(AB - BA)' = (AB)' - (BA)'$$

$$= B'A' - A'B'$$

$$= BA - AB$$

$$= -(AB - BA)$$

Hence, $(AB - BA)$ is a skew symmetric matrix.

Q7. What are the possible orders if a matrix has 28 elements?

- (a) 5 (b) 6 (c) 4 (d) 7

Ans: (b) 6

Explanation:

The possible orders are

1 x 28, 2 x 14, 4 x 7, 7 x 4, 14 x 2, 28 x 1.

Q8. If A is a square matrix, then $A - A'$ is a

- (a) Skew-symmetric matrix
(b) Symmetric matrix
(c) Diagonal matrix
(d) None of these

Ans: (a) Skew-symmetric matrix

Explanation: It is given that A is a square matrix

Now transpose of $A - A'$

$$(A - A')'$$

$$A' - (A')'$$

$$A' - A = -(A - A')$$

It is skew symmetric

INSTRUCTIONS FOR Q9 AND Q10

The following questions consist of two statements – Assertions (A) and Reason(R). Answer these questions selecting the appropriate option given below:

- (a) Both A and R are true and R is the correct explanation for A
(b) Both A and R are true and R is not the correct explanation for A
(c) A is true but R is false
(d) A is false but R is true

Q9. Assertion (A): Every identity function is one-one and onto.

Reason (R): An identity function maps each element to itself.

Ans. Option (a) is correct.

Explanation: The identity function satisfies both injectivity (one-one) and surjectivity (onto), and the reason correctly supports this.

Q10. Assertion: $\sin^{-1}(\sin 2\pi/3) = \pi/3$

Reason: $\sin^{-1}(\sin \theta) = \theta$, when $\theta \in [-\pi/2, \pi/2]$

Ans. Option (a) is correct.

Explanation: The principal branch of \sin^{-1} is $[-\pi/2, \pi/2]$, and $\pi/3 \in [-\pi/2, \pi/2]$